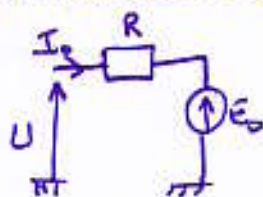


A) Etude du moteur

I. Essai à vide

$$U = 220V, I_0 = 17,5mA, n_0 = 3400 \text{ tr/min.}$$

A.1.1. Calcul de E_0 :



$$U - RI_0 - E_0 = 0.$$

$$E_0 = U - RI_0.$$

$$= 220 - 42 \times 17,5 \cdot 10^{-3} = 199V.$$

$$E_0 = 199V.$$

A.1.2. Calcul de P_0 :

$$P_0 = UI_0 = 3,3W$$

A.1.3. Calcul de P_{J_0} :

$$P_{J_0} = RI_0^2 = 42 \times (17,5 \cdot 10^{-3})^2 = 0,01286W$$

$$P_{J_0} = 12,9 \text{ mW}$$

A.1.4. Calcul de P_c :

Bilan de puissance:

$$P = UI = R I^2 + P_c + P_u.$$

$$\text{A vide: } P_u = 0$$

$$P_0 = UI_0 = RI_0^2 + P_c.$$

$$\text{donc } P_c = UI_0 - RI_0^2 = I_0(U - RI_0)$$

$$P_c = 3,49W.$$

A.1.5. Calcul de T_p :

$$P_c = T_p \omega$$

$$T_p = \frac{P_c}{\omega} = \frac{P_c}{\frac{2\pi n_0}{60}}$$

$$T_p = 0,0098 \text{ N.m}$$

II. Essai en charge

$$U = 200V, I = 0,8A$$

A.2.1. Calcul de E :

$$E = U - RI = 200 - 42 \times 0,8 = 166,4V$$

A.2.2. Calcul de n :

$$\left. \begin{array}{l} \text{A vide: } E_0 = k\phi n_0 \\ \text{En charge: } E = k\phi n \end{array} \right\} n = \frac{E}{E_0} n_0 = \frac{166}{199} \times 3400$$

$$n = 2843 \text{ tr/min}$$

A.2.3. Calcul de Γ_{em} :

$$P_{em} = E I = \Gamma_{em} \omega$$

$$\Gamma_{em} = \frac{EI}{\omega} = \frac{EI}{\frac{2\pi n}{60}} = 0,447 \text{ N.m}$$

A.2.4. Calcul de Γ_u :

$$\text{Bilan de puissance: } P_u + P_c + RI^2 = UI$$

$$P_u = \Gamma_u \omega = UI - P_c - RI^2$$

$$\Gamma_u = \frac{UI - P_c - RI^2}{\frac{2\pi n}{60}} = 0,435 \text{ N.m}$$

A.2.5. Calcul du Rendement η :

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$$\eta = \frac{P_u}{P_{abs}} = \frac{P_u}{UI} = \frac{I_{ucl}}{UI}$$

$$\eta = 0,809. \quad \eta = 80,9\% \approx 81\%$$

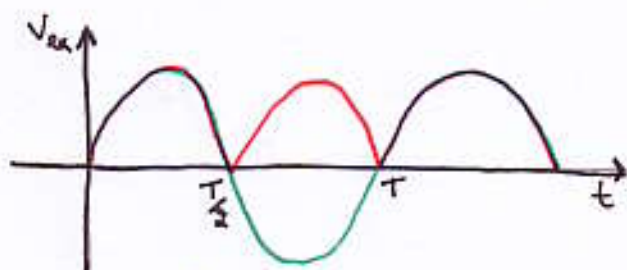
B) Etude de l'alimentation du moteur

$$f = 50 \text{ Hz} \quad V = 220 \text{ V}$$

I. Alimentation de l'inducteur

B.1.1. Voir courbe.

- Si $i > 0$ alors D_1 et D_3 conduisent (D_2 et D_4 bloquées) donc $V_{ex} = U$.
- Si $i < 0$ alors D_2 et D_4 " (D_3 et D_1 ") donc $V_{ex} = -U$



B.1.2.

$$\textcircled{1} \quad \overline{V_{ex}} = \frac{1}{\frac{T}{2}} \int_0^{\frac{T}{2}} U \sin \omega t \, dt = \frac{2U}{T} \left[-\frac{\cos \omega t}{\omega} \right]_0^{\frac{T}{2}}$$

$$\overline{V_{ex}} = \frac{2U}{\frac{2\pi}{\omega} \times \omega} \times \left(-\cos \frac{2\pi}{T} \times \frac{T}{2} + \cos 0 \right) = \frac{U}{\pi} (1 + 1) = \frac{2U}{\pi} = 198 \text{ V}$$

$$\textcircled{2} \quad U_{ex}^2 = \frac{1}{\frac{T}{2}} \int_0^{\frac{T}{2}} (U \sin \omega t)^2 \, dt$$

$$= \frac{2}{T} \times U^2 \times \int_0^{\frac{T}{2}} \left(\frac{1}{2} (1 - \cos 2\omega t) \right) dt = \frac{2U^2}{T} \left[t - \frac{\sin 2\omega t}{2\omega} \right]_0^{\frac{T}{2}}$$

$$U_{ex}^2 = \frac{2U^2}{T} \left(\frac{T}{2} - \frac{\sin (2 \times \frac{2\pi}{T} \times \frac{T}{2})}{\frac{2 \times 2\pi}{T}} - 0 + \frac{\sin 0}{\frac{2 \times 2\pi}{T}} \right)$$

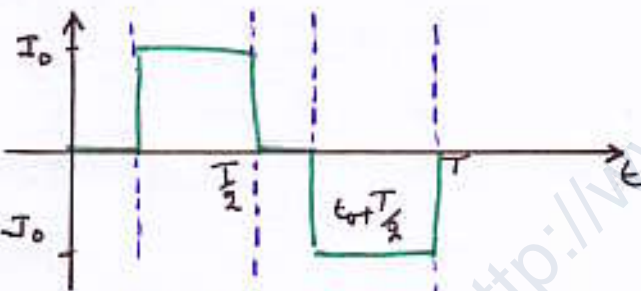
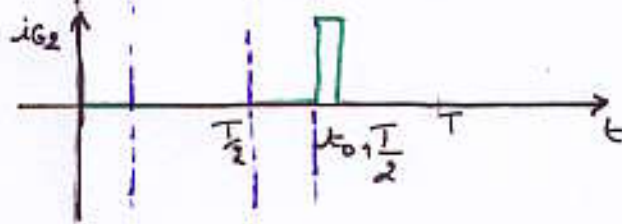
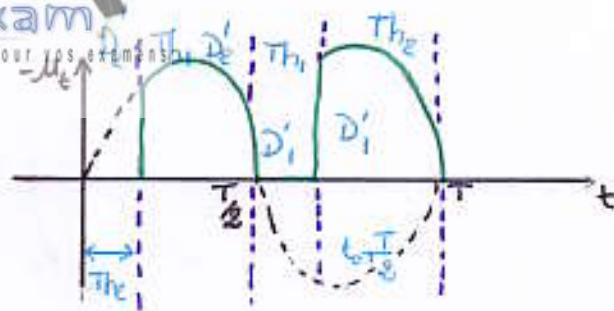
$$U_{ex}^2 = U^2 \left(1 - \frac{\sin 2\pi}{2\pi} \right)$$

$$U_{ex}^2 = U^2$$

$$U_{ex} = U.$$

II. Alimentation de l'induit.

B.2.1. Voir page suivante.



B.2.2. $\bar{U} = \frac{220\sqrt{2}}{\pi} (1 + \cos \theta_0)$

Si $\bar{U} = 150 \text{ V}$ $150 = \frac{220\sqrt{2}}{\pi} (1 + \cos \theta_0) \Rightarrow \frac{150\pi}{220\sqrt{2}} - 1 = \cos \theta_0$

$\theta_{\text{rad}} = \arccos\left(\frac{150\pi}{220\sqrt{2}} - 1\right) = 1,03 \text{ rad} = 59^\circ$

c) Neutre du couple. $\Delta R = \frac{k' F R_0}{S}$ $k' = 10^{-10} \text{ m}^2/\text{N}$
 $S = 5 \cdot 10^{-4} \text{ m}^2$

c.1: Calcul de R_0 :

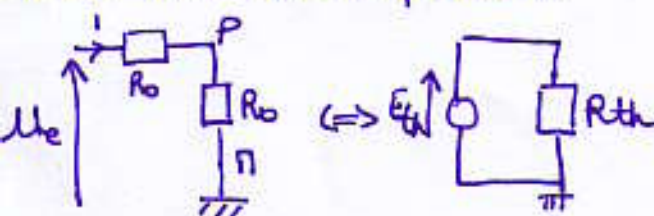
la jauge est assimilée à un fil résistif $\rho = 10^{-6} \Omega/\text{m}$ $l = 5 \cdot 10^{-3} \text{ m}$

$R_0 = \rho \frac{l}{S} = 250 \Omega$

c.2. Calcul de ΔR : $F = 500 \text{ N}$

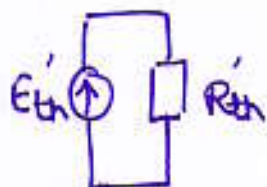
$\Delta R = \frac{k' F R_0}{S} = \frac{10^{-10} \times 500 \times 250}{5 \cdot 10^{-4}} = 25 \text{ m}\Omega$

c.3. NET du dipôle PT:



$R_{th} = \frac{R_0}{2}$

$E_{th} = \frac{R_{th} u_e}{2 R_0} = \frac{u_e}{2}$



$$E'_{th} = \frac{R_1 u_e}{R + R_0}$$

$$R'_{th} = \frac{R R_0}{R + R_0}$$

. C.5. AOP idéal $i_+ = i_- = 0$

AOP en linéaire: $E = 0$ $v^+ = v^-$

or $v^+ = \frac{R_3 u_2}{R_3 + R_2}$ et $v^- = \frac{u_1 R_3 + v_3 R_4}{R_3 + R_4}$

donc $\frac{R_3 u_2}{R_3 + R_2} = \frac{R_3 u_1 + R_4 v_3}{R_4 + R_3}$ et $u_3 = \frac{R_3 (R_4 + R_3)}{R_4 (R_3 + R_2)} u_2 - \frac{R_3}{R_4} u_1$

. C.6. $u_3 = 10^3 \left(\frac{R - R_0}{R + R_0} \right) u_e$ $R = R_0 + \Delta R$

$$u_3 = 10^3 \left(\frac{R_0 + \Delta R - R_0}{R_0 + \Delta R + R_0} \right) u_e = 10^3 \left(\frac{\Delta R}{2R_0 + \Delta R} \right) u_e$$

$$u_3 = 10^3 \left(\frac{1}{1 + 2 \frac{R_0}{\Delta R}} \right) u_e = 10^3 \left(\frac{1}{1 + 2 \frac{R_0 \times 5}{k' F R_0}} \right) u_e$$

$$u_3 = 10^4 \left(\frac{1}{1 + \frac{25}{k' F}} \right) u_e = 10^{-3} F \text{ avec } R_0 \gg \Delta R$$

AN: $u_3 = 10^4 \left(\frac{1}{1 + \frac{2 \times 5 \cdot 10^{-4}}{10^{-10} \times 500}} \right) = 0,499 V$

$$u = 0,5 V.$$